

basics, measurement and modelling of BRTF

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1 basics

- introduction
- photometrics reloaded

2 BRTF math

- BRTF definition

3 gonio-photometers

- incidence light
- sample mount
- detector system

4 BRTF data and models

- example data BRTF
- asymmetric in/out angular resolution

5 getting BRTF into *Radiance*

- paths
- BRTF models
- example: model fits in 1994
- what *Radiance* is missing

- BR_{TF} = bidirectional reflection transmission function
- BS_{DF} = bidirectional scatter distribution function
- B_{xxx} = .. whatever..

all the same quantity:

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- BS_{DF} = bidirectional scatter distribution function
- B_{xxx} = .. whatever..

all the same quantity:
scattering of light at a surface

what is this talk about ?

- sequence to simulation results:

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- 2 model material

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- 3 add geometry, sky, etc

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BRDF depends on surface finish

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BRTF depends on surface finish
- 3 manufacturers specs not always available
- 4 recheck manufacturers specs
- 5 compare materials by BRTF data

solid angle

- solid angle of an object as seen from point P :
project object onto sphere with radius r around P
$$\Omega := \frac{A_p}{r^2}$$
- unit: *steradian* [sr]
- dimensionless, full sphere: 4π , hemisphere: 2π
- infinitesimal: $d\Omega$, finite: Ω or $\Delta\Omega$
- solid angle of a cone with opening angle α :
$$\Omega_{\text{cone}} = 2\pi \left(1 - \cos \frac{\alpha}{2}\right)$$

radiant power

basic unit:

power transported by electromagnetic radiation

as described within concept of *photometry*
(sometimes known as *radiance flux*)

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three spectral flavours:

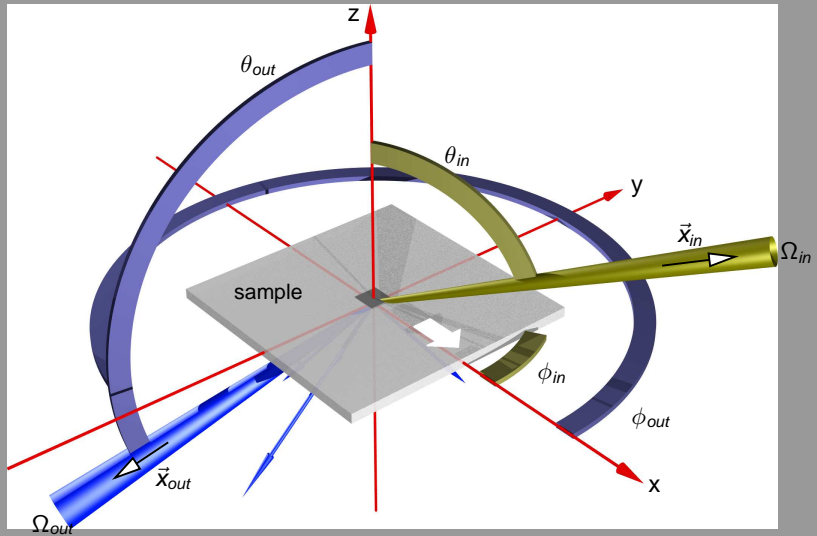
- spectrally integrated: *radiometric* [Watt]
- spectrally resolved: power per wavelength interval [Watt/nm]
- weighted by eye response and integrated: *photometric* [Lumen]

quantities used most often:

- radiant power per area: \mathcal{E} [Watt/m²]
- radiant power per solid angle [Watt/sr] (*Radiant Intensity*)
- radiant power per solid angle and projected area, $\mathcal{L}(\vec{x})$, [Watt/(sr*m²)] (*Radiance*)

... and equivalent photometric units

coordinate system



advantages of using these sample coordinates:

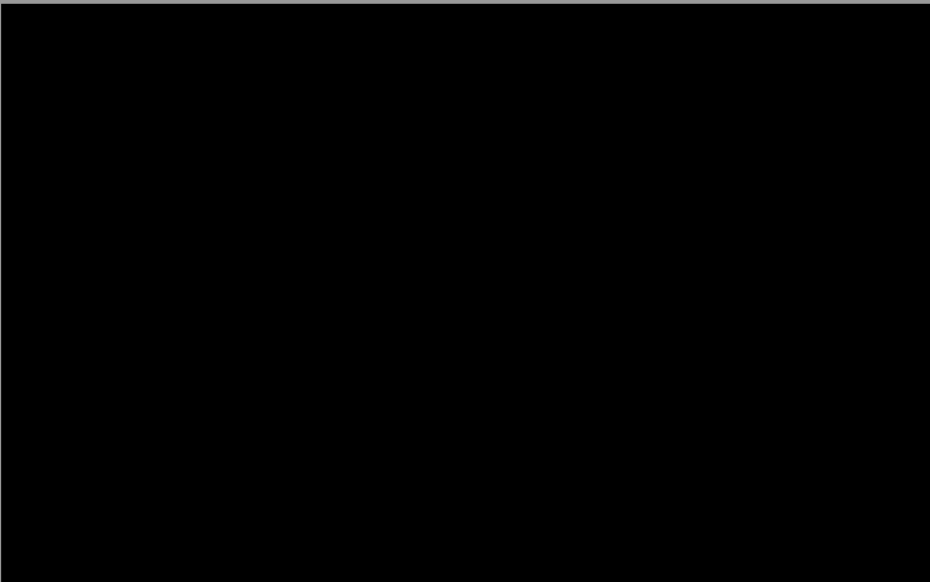
- standard polar coordinates
- one BRDF for front and back side of sample
- z-axis: surface normal
x-axis: marked on sample
- direction written as \vec{x} or (θ, ϕ)

With incident light on the *front* surface: $\theta_{in} = (0^\circ \dots 90^\circ)$:

- $\theta_{out} = (0^\circ \dots 90^\circ)$ reflection,
 $\theta_{out} = (90^\circ \dots 180^\circ)$ transmission.

Other coordinates possible, use transformations.

it's all easy ...



Definition

$$\mathcal{L}_{out}(\vec{x}_{out}) = \int_{\vec{x}_{in}}^{\Omega_{in}=2\pi} BRTF(\vec{x}_{out}, \vec{x}_{in}) \mathcal{L}_{in}(\vec{x}_{in}) \cos(\alpha_{in}) d\Omega_{in}$$

defining formula

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- $BRTF_{void}(\vec{x}_{out}, \vec{x}_{in}) = \delta(\vec{x}_{out} - \vec{x}_{in}) / \cos(\alpha_{in})$, *Dirac Delta function*
- $BRTFc(\vec{x}_{out}, \vec{x}_{in}) := BRTF(\vec{x}_{out}, \vec{x}_{in}) \cos(\alpha_{in})$

approximate formula

$$\mathcal{L}_{out}(\vec{x}_{out}) = \int_{\vec{x}_{in}}^{\Omega_{in}=2\pi} \textcolor{red}{BRTF}(\vec{x}_{out}, \vec{x}_{in}) \mathcal{L}_{in}(\vec{x}_{in}) \cos(\alpha_{in}) d\Omega_{in} \quad (1)$$

- assume $\mathcal{L}_{in} > 0$ for small Ω_{in} around \vec{x}_{in}^* only
- and assume $BRTF = \text{const}$ over Ω_{in}

approximate formula

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- assume $\mathcal{L}_{in} > 0$ for small Ω_{in} around \vec{x}_{in}^* only
- and assume $BRTF = \text{const}$ over Ω_{in}
- then, and only then

$$BRTF(\vec{x}_{out}, \vec{x}_{in}^*) \approx \frac{\mathcal{L}_{out}(\vec{x}_{out})}{\mathcal{E}_{in}} \quad (2)$$

But:

This approximation is misleading and should be used with **caution**.

measured BRTF is always averaged over solid angles of detector $\Delta\Omega_{out}$ and lamp $\Delta\Omega_{in}$:

$$\overline{BRTF}(\Delta\Omega_{in}, \Delta\Omega_{out}) := \frac{1}{\Delta\Omega_{in} \Delta\Omega_{out}} \int_{\vec{x}_{out}}^{\Delta\Omega_{out}} \int_{\vec{x}_{in}}^{\Delta\Omega_{in}} BRTF(\vec{x}_{out}, \vec{x}_{in}) d\Omega_{in} d\Omega_{out} \quad (3)$$

consequences:

this limit measurement of BRTF features.

\rightsquigarrow minimise $\Delta\Omega_{out}$ and $\Delta\Omega_{in}$

transmission τ from Ω_{in} into Ω_{out} is given by:

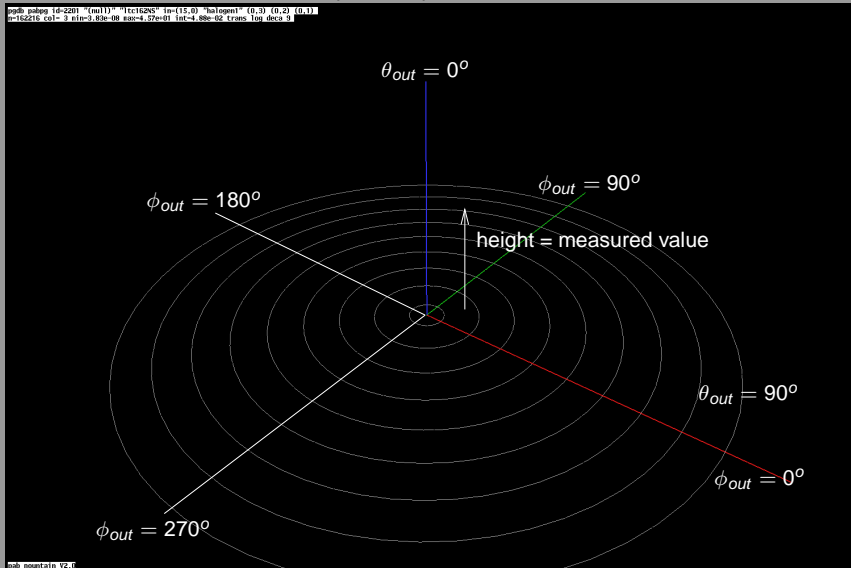
$$\tau(\Omega_{in}, \Omega_{out}) = \frac{\int_{\vec{x}_{out}}^{\Omega_{out}} \left\{ \int_{\vec{x}_{in}}^{\Omega_{in}} BRTF(\vec{x}_{out}, \vec{x}_{in}) \mathcal{L}_{in}(\vec{x}_{in}) \cos(\alpha_{in}) d\Omega_{in} \right\} \cos(\alpha_{out}) d\Omega_{out}}{\int_{\vec{x}_{in}}^{\Omega_{in}} \mathcal{L}_{in}(\vec{x}_{in}) \cos(\alpha_{in}) d\Omega_{in}} \quad (4)$$

Which for the *direct-hemispherical transmission* results in:

$$\tau_{dh}(\vec{x}_{in}) := \tau(d\Omega_{in}, 2\pi) = \int_{\vec{x}_{out}}^{2\pi} BRTF(\vec{x}_{out}, \vec{x}_{in}) \cos(\alpha_{out}) d\Omega_{out} \quad (5)$$

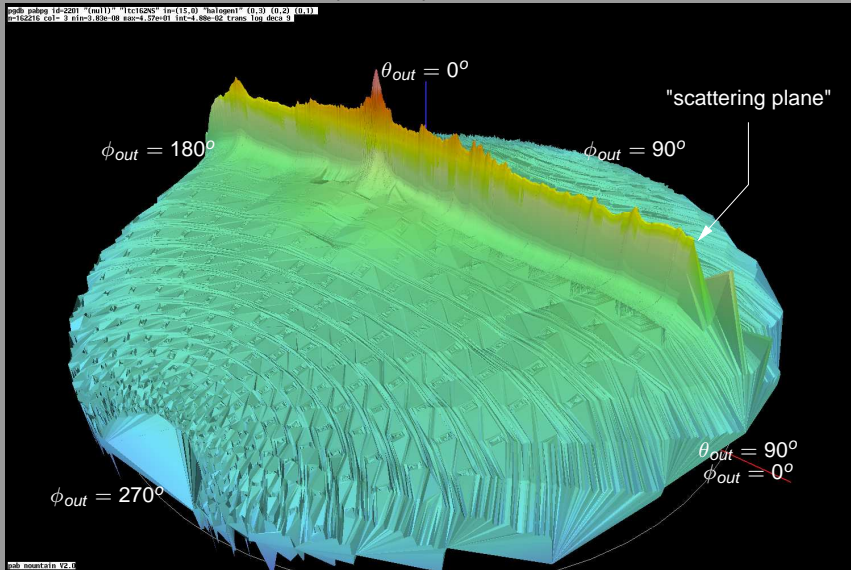
visualising BRTF 3D

for one incident direction (θ_{in}, ϕ_{in}) , display one hemisphere:



visualising BRTF 3D

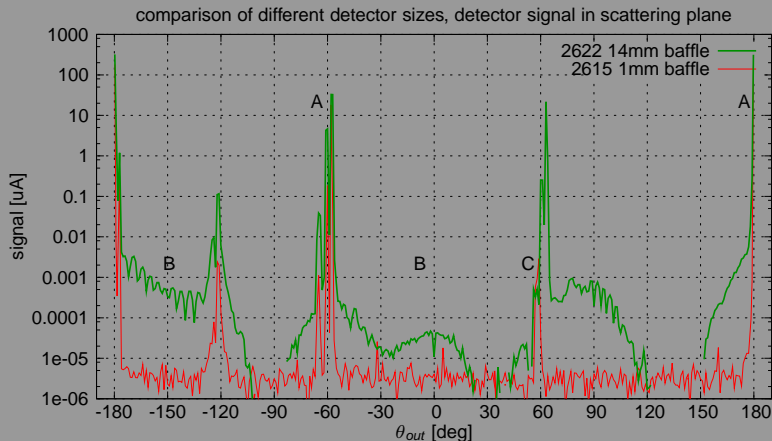
for one incident direction (θ_{in}, ϕ_{in}), display one hemisphere:



visualising BRTF 2D

2D cuts along scattering plane through 3D dataset

I prefer Cartesian plots over polar plots. example:



... questions to math part ?

next to come: gonio-photometers

light source types & parameters

beam parameter	Halogen	Xenon	laser diode	gas laser
power	+	++	-	-
radiance	-	+	++	+++
noise	++	+	+	+
polychromatic	+	+	-	-
incoherent	+	+	-	-

choice depends on:

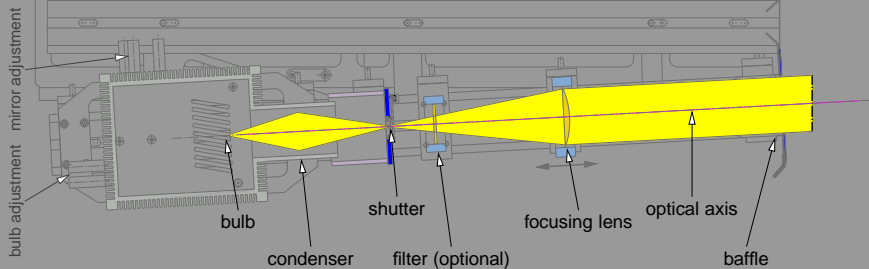
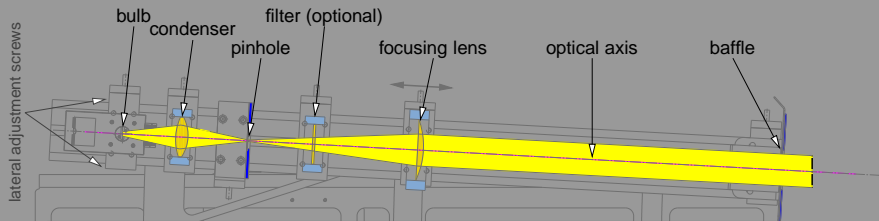
- sample type
- wavelength range
- detector type

in the following: lamps kept at fixed positions

alternative concepts: moving lamp, fixed sample

example: pgl lamp subsystem

Halogen subsystem

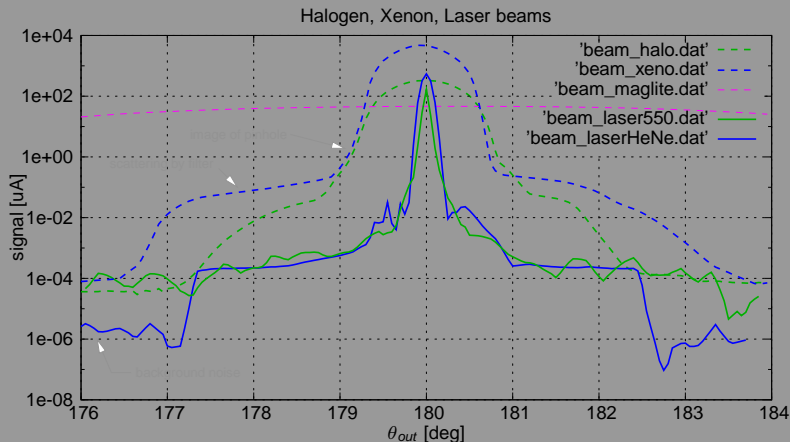


Xenon subsystem

example: pgl lamp subsystem



example: beam profiles



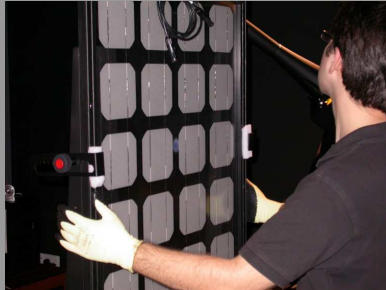
- fixes sample (securely)
- adjusts for θ_{in}, ϕ_{in}
- \rightsquigarrow two degrees of freedom
manual adjustment or automatic
- minimal self-shadowing
- shading of stray light

in the following: vertical sample mount assumed

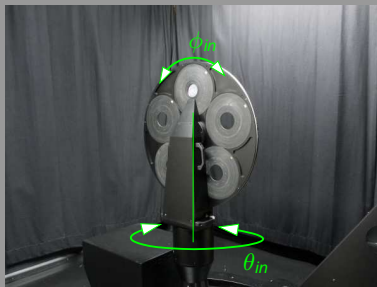
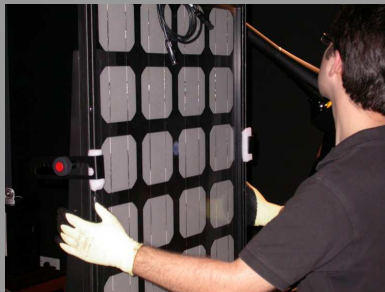
example sample mounts

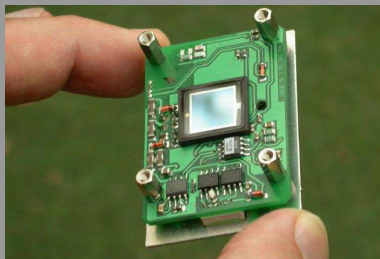


example sample mounts

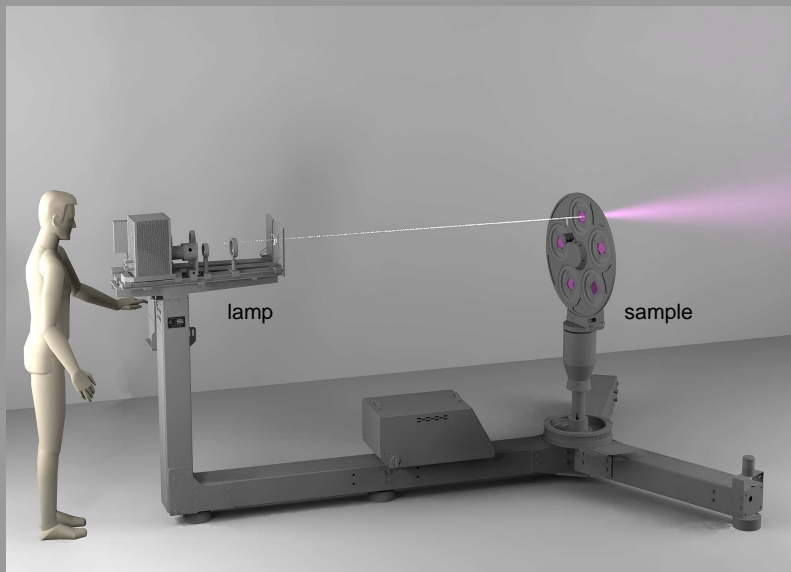


example sample mounts

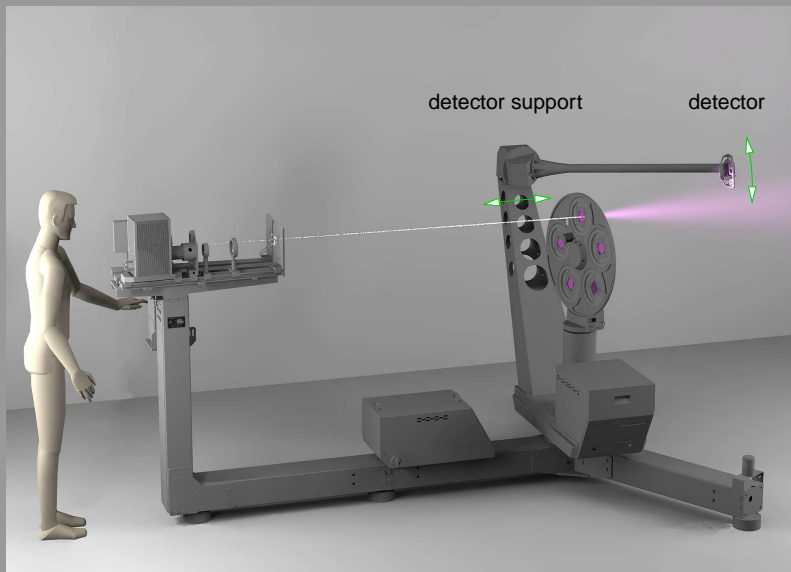




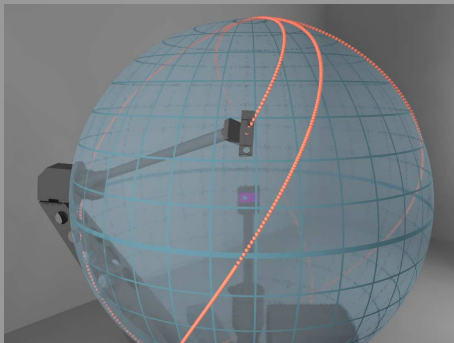
- material and wavelength: Si (VIS), InGaAs (IR), etc
- principle: photo-diode, etc
- sample rate: measurements / second: 1Hz to 1kHz
- noise: *noise equivalent BRTF*, lowest measurable BRTF
- dynamic range: 10^2 at least, 10^8 better



detector mechanics



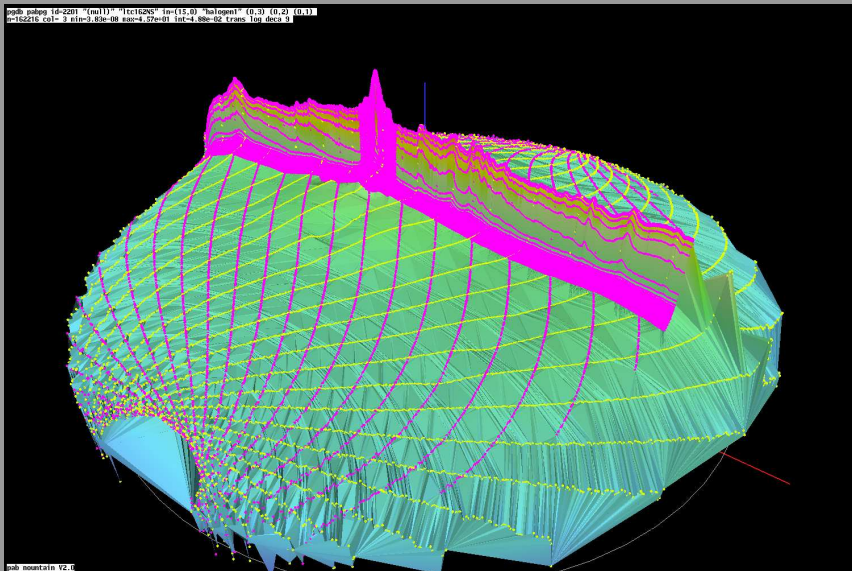
scanning gonio-photometer



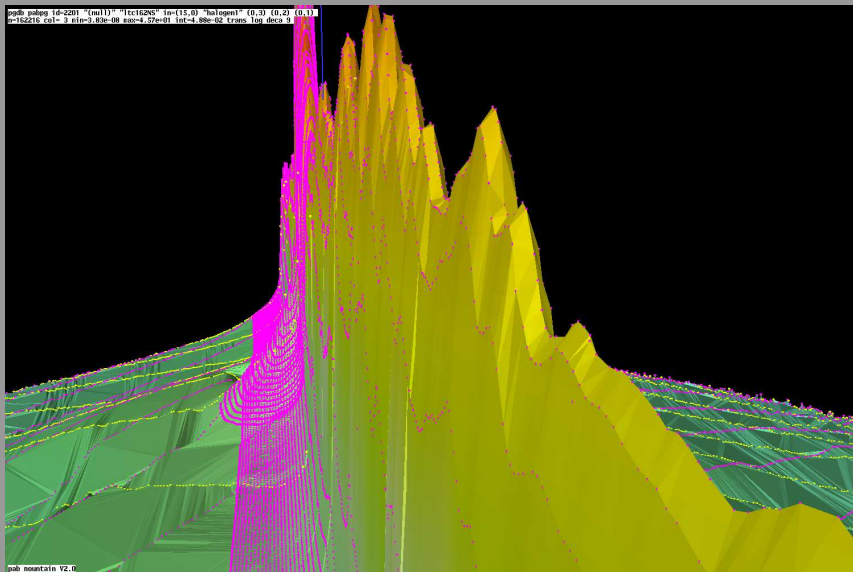
measurements-on-the-fly:

- avoid start-stop-cycles
- need excellent sync between position and data-acquisition
- need fast detector

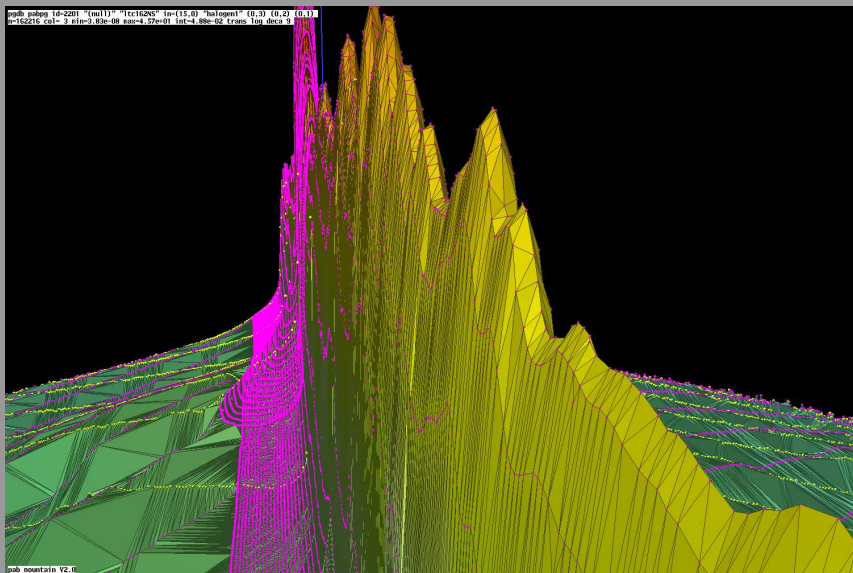
discrete BRTF values versus continuous function



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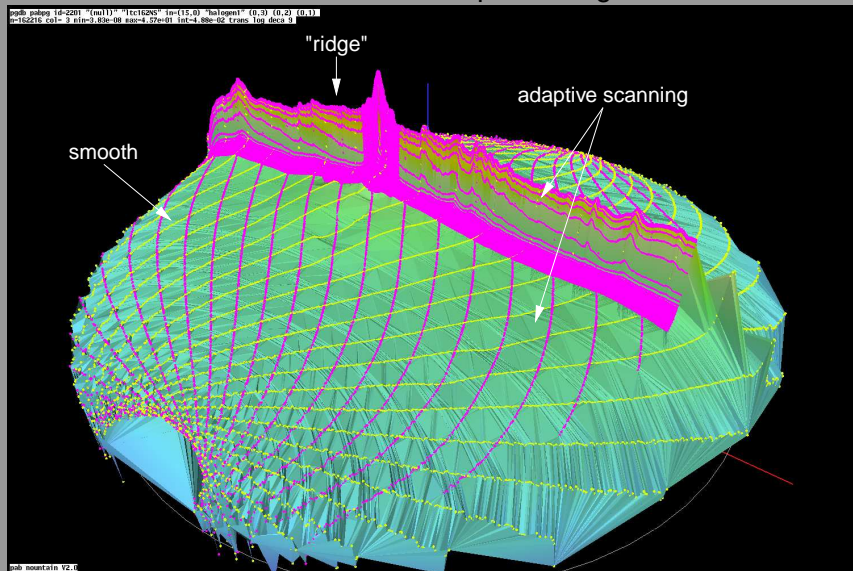


discrete BRTF values versus continuous function

- in 3D, $f(x_i, y_i)$ data points
do *not* define a unique surface
- Delaunay triangulation recommended
- triangulation used for interpolation and integration
- \rightsquigarrow good triangulation vital for BRTF data processing

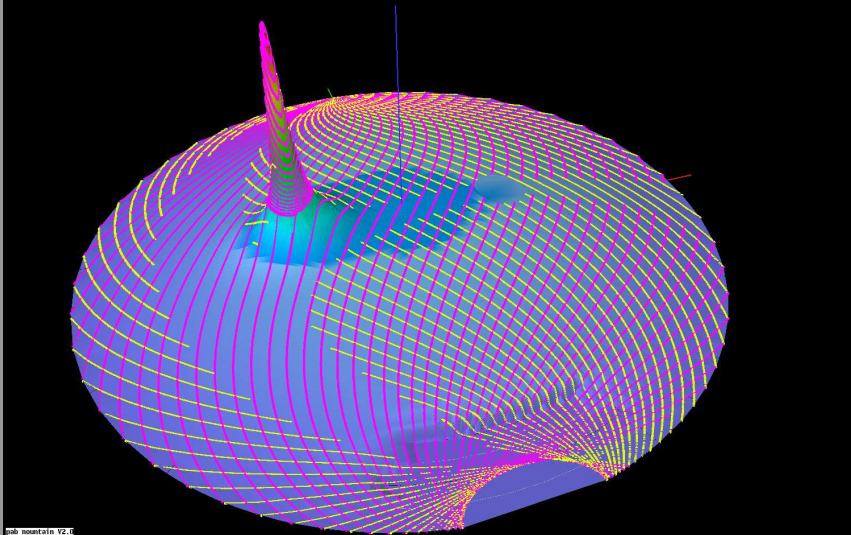
adaptive high angular resolution

BRTF consists of smooth areas and peaks/ridges:



checking for measurement errors implicitly

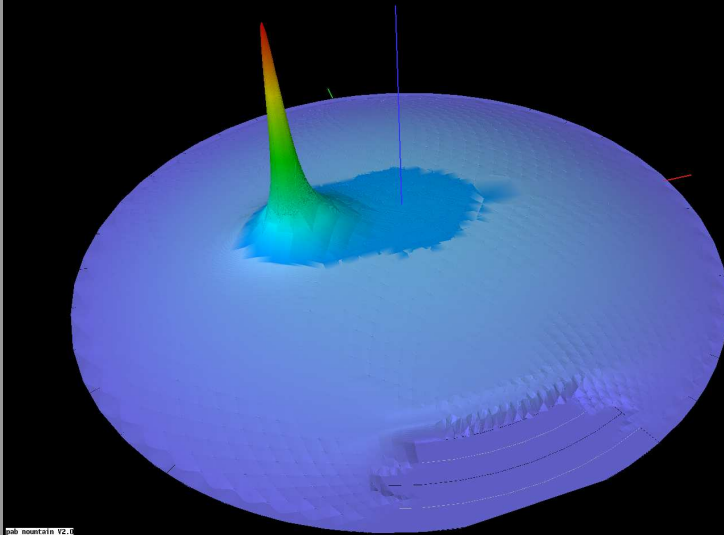
```
pdb> psbpa id=2750 "P11002CRAP10" "P11002CRAP10" in=(30,0) "halogen1" (0,3) (0,2)  
n=124889 col= 3 efm=4.07e-09 sas=5.40e-01 int=2.88e-01 refl lin
```



128109 data points all nicely smooth

checking for measurement errors implicitly

```
pab: pabeg id=2750 "P11002CRAP10" "P11002CRAP10" in=(30,0) "halogen1" (0,3) (0,2)  
n=124889 col= 3 efn=4.07e-09 sas=5.40e-01 int=2.89e-01 refl lin
```

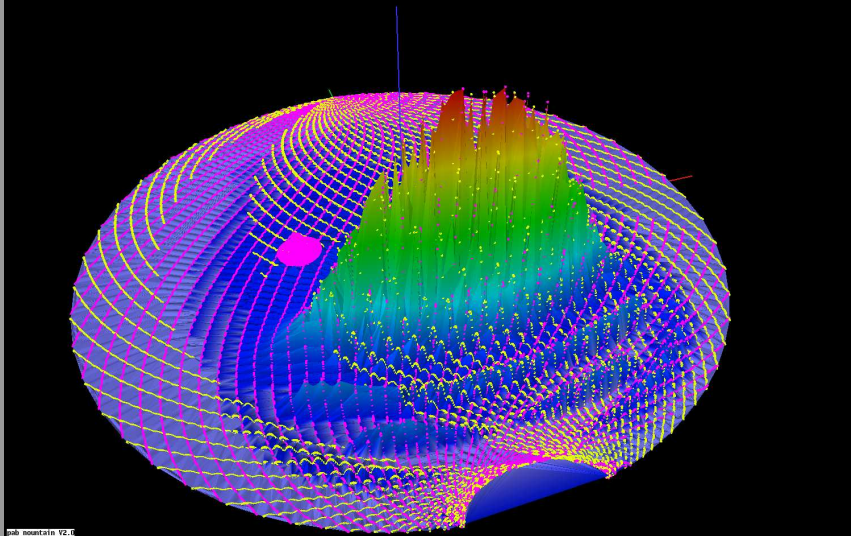


mob mountain V2.0

good.

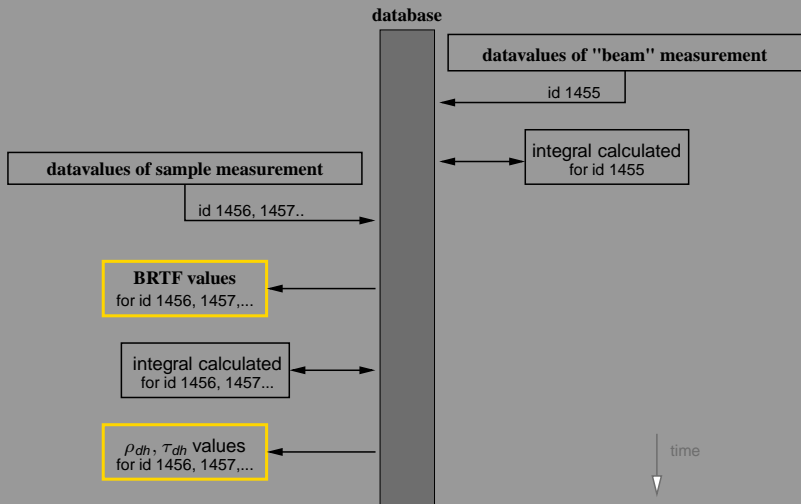
checking for measurement errors implicitly

```
pdb> pabpa id=2753 "P11002CRAP10" "P11002CRAP10" in=(30,0) "halogen1" (0,3) (0,2)  
n=128194 col= 3 pin=8.06e-03 sas=4.39e+00 int=1.17e+00 refl lin
```



ceiling lights on, 100Hz noise, (see SPIE 2010 paper for more)

getting BRTF from raw data



advantages of using unscattered beam as reference

- illuminated area and detector distance cancel out
- no reference samples needed
- sensor identical for reference measurement

imaging versus scanning gonio-photometers

alternative way of doing measurements:

imaging gonio-photometers

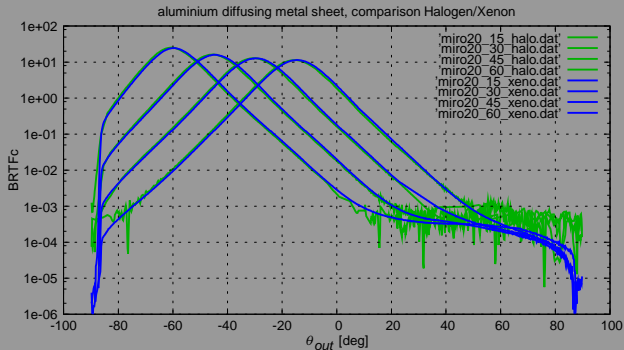
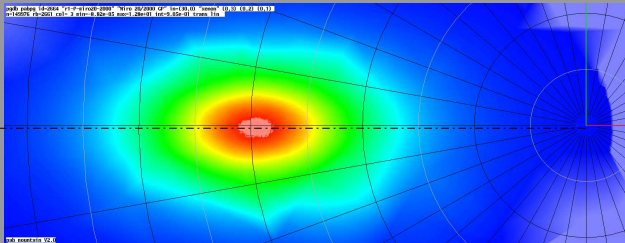
- + faster
- - more intermediate optics, not as general

very short intermission

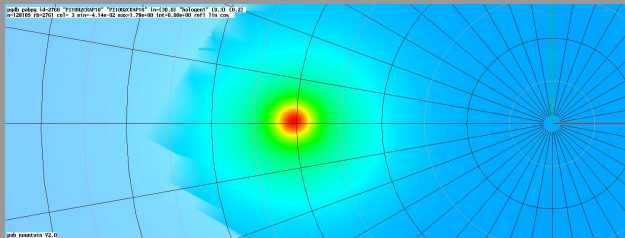
... questions to machine&measurement part ?

next to come: BRTF data &models

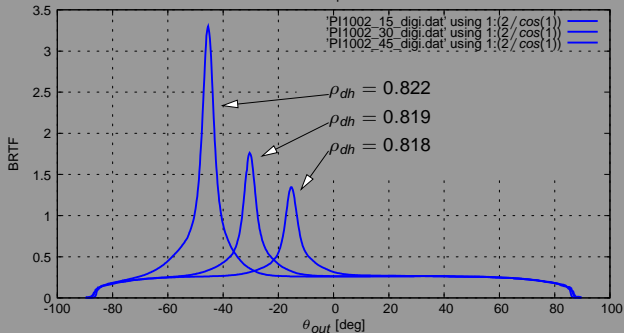
example: aluminium



example: white paint

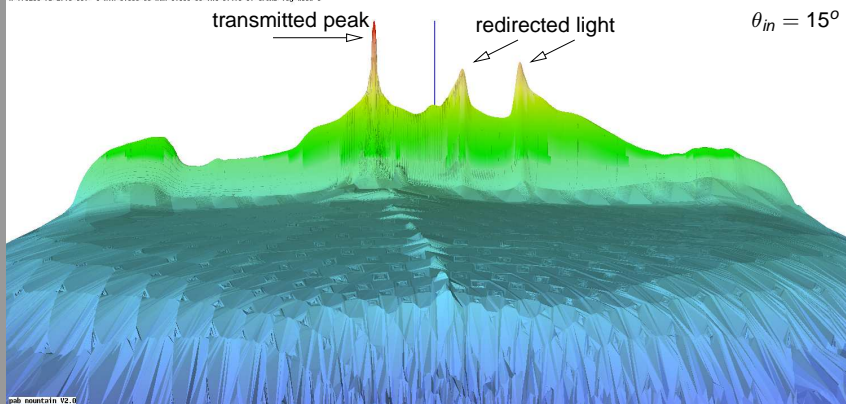


white paint

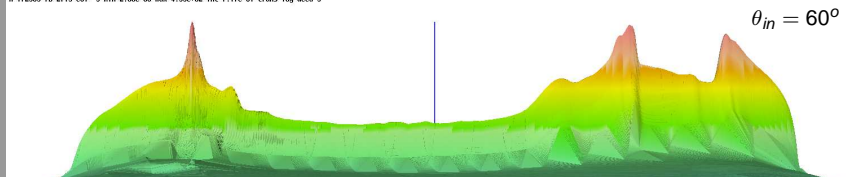


example: light redirecting, Serraglaze

```
pgdb pabpg id=2716 "serraglaze1" "serraglaze laminated file" in=(15,0) "xenon" (0,3) (0,2) (0,1) (0,0)  
n=176208 rb=2715 col= 3 nin=5.68e-09 mac=9.96e-03 int=8.41e-01 trans log deca 9
```



```
pgdb pabpg id=2719 "serraglaze1" "serraglaze laminated file" in=(60,0) "xenon" (0,3) (0,2) (0,1)  
n=172985 rb=2715 col= 3 nin=2.00e-08 mac=4.39e-02 int=7.17e-01 trans log deca 9
```



angular resolution of incident and outgoing side

both sides are *not* symmetric:

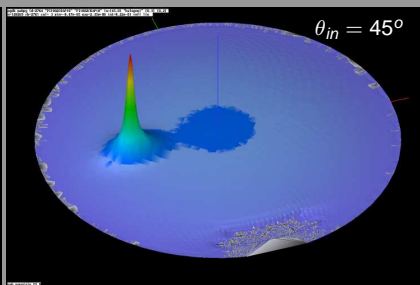
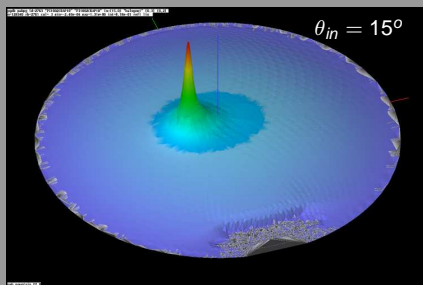
- outgoing side:
adaptive, high resolution (0.1°)
- incident side:
low resolution (10°)

since:

Theorem

in most cases the topology of a BRTF does not change between \vec{x}_{in} and $\vec{x}_{in} + \Delta$, for small Δ (e.g. 20°)

topology of a BRTF



- structure ("topology") of BRTF remains the same for Δ
- shape *parameters* change:
peak position, peak height, peak width, background level
- \rightsquigarrow intermediate θ_{in} are predictable.
- \rightsquigarrow measurements of finely resolved θ_{in} are redundant
- \rightsquigarrow don't waste time and data with these
think of a good interpolation method

getting BRTF into *Radiance*

problems to solve while importing data:

- interpolation between outgoing directions \vec{x}_{out} :
triangulation, etc

getting BR_{TF} into *Radiance*

problems to solve while importing data:

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triangulation, etc
- interpolation between incident directions \vec{x}_{in} :
not a trivial problem

getting BRTF into *Radiance*

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triangulation, etc
- interpolation between incident directions \vec{x}_{in} :
not a trivial problem
- optional data compression

getting BRTF into *Radiance*

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ways into simulation program

getting BRTF into *Radiance*

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triangulation, etc
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not a trivial problem
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ways into simulation program

- loading BRTF data-files directly

getting BRTF into *Radiance*

problems to solve while importing data:

- interpolation between outgoing directions \vec{x}_{out} :
triangulation, etc
- interpolation between incident directions \vec{x}_{in} :
not a trivial problem
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ways into simulation program

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loading BRDF data-files directly

problems:

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fitting parameter of function to BRTF data

process:

- fit $f_{a_1 \dots a_N}(\theta_{out}, \phi_{out})$ to one dataset of incident direction \vec{x}_{in}

note: see chapter 5 in author's 1995 dissertation (in German)

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drawbacks:

- requires that f and choice of $a_1 \dots a_N$ describe scattering well

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fitting parameter of function to BRDF data

process:

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- standard Levenberg-Marquardt method not 100% robust

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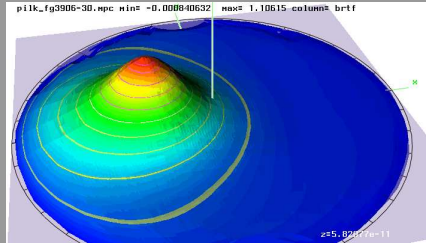
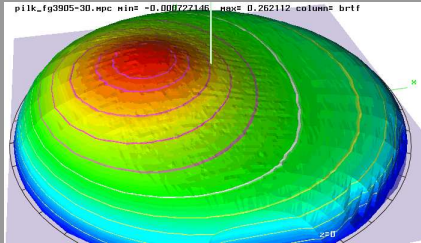
- internal to *Radiance* (e.g. trans)

$$BRTF_{trans} = \frac{a_6 (1 - a_7)}{\pi} + \frac{a_6 a_7}{\pi a_5^2 \sqrt{\cos(\theta_{in}) \cos(\theta_{out})}} \exp[(2 \cos(\theta_{half}) - 2)/a_5^2] \quad (6)$$

- external (example)

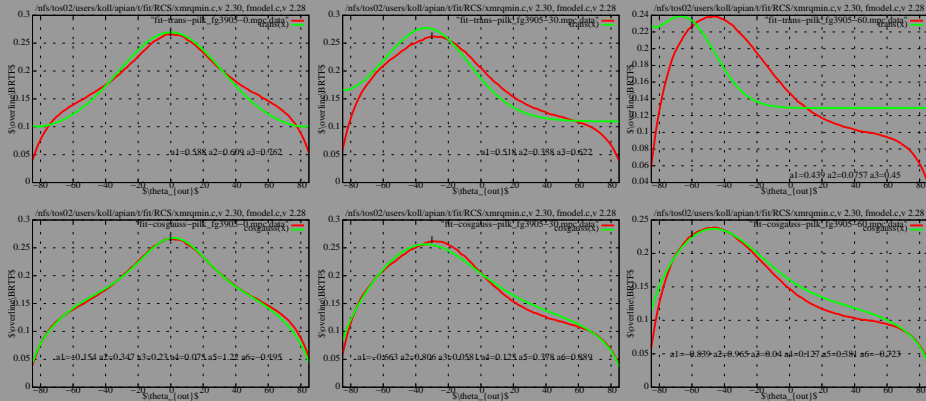
$$\begin{aligned} BRTF_{cosgauss} &:= a_1 + a_2(\cos \theta)^{a_3} + a_4 \exp(-\beta^2 a_5) & (7) \\ \beta &:= \arccos[\cos(\theta) \cos(\alpha_{in} + a_6) - \sin(\theta) \cos(\phi_{out}) \sin(\alpha_{in} + 10a_6)] \\ \theta &:= \pi - \theta_{out} \end{aligned}$$

example: fits to Pilkington fg3905, fg3906 in 1994



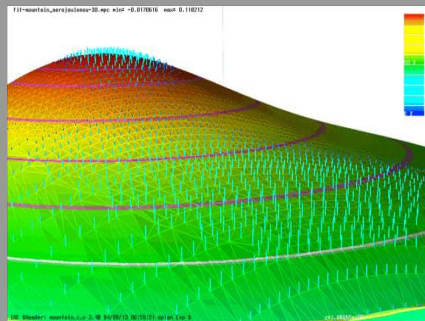
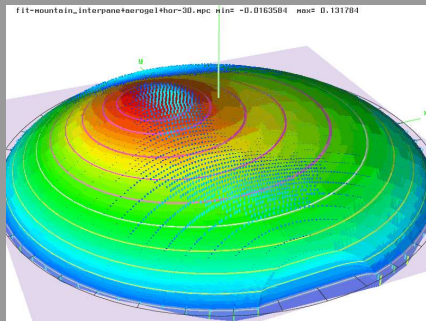
polymer/glass sandwich glazing,
forward scattering, "milky" glazing

fg3905 model comparison, in scattering-plane



note: see chapter 6 in author's 1995 dissertation for details

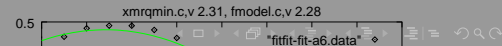
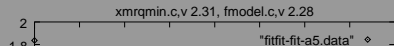
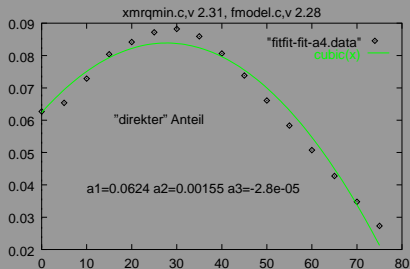
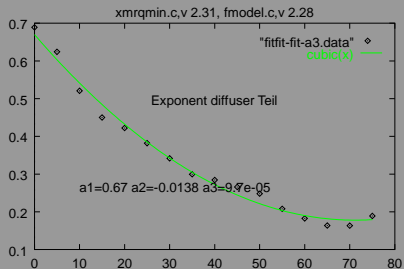
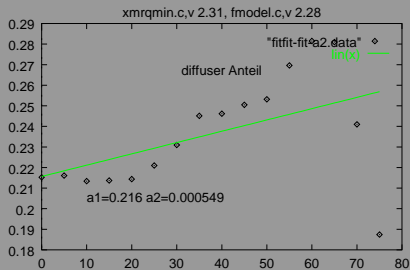
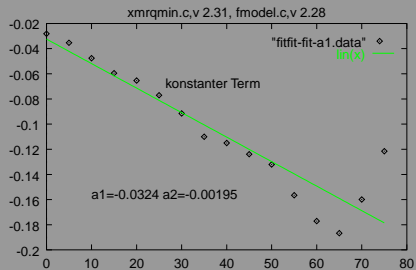
fg3905 model comparison, off scattering-plane



deviation between model and data shown as spikes

fitting is done for all outgoing directions (not just in-plane)
model may deviate outside the scattering plane

example: Aerogel model, parameter variation



- current models don't match measured data well

conclusions for *Radiance* models

- current models don't match measured data well
- better built-in models or cal-files seem worth considering

what *Radiance* is missing

- cal file support for photon-map (and ambient calcs)
 - ~> support for general BRTF models

all these features require changes to the rendering core

~> non trivial work. But would be *very* useful in practice.

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what *Radiance* is missing

- cal file support for photon-map (and ambient calcs)
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- BRTF import using non-fixed-grid data
- way to add internal models in a modular way

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latest papers on pgII gonio-photometer & links:

- "Experimental validation of bidirectional reflection and transmission distribution measurements of specular and scattering materials,"
SPIE 2010, Brüssel, <http://dx.doi.org/10.1117/12.860889>
- "New scanning gonio-photometer for extended BRTF measurements"
SPIE 2010, San Diego, <http://dx.doi.org/10.1117/12.854011>
- currently installed pgII gonio-photometers:
SERIS Singapore, LBNL Berkeley, pab Freiburg, industrial client Europe
- pgII gonio-photometer webpage:
<http://www.pab.eu>
- author's 1995 Phd: <http://www.pab-opto.de/pers/phd/>

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last slide.

- physics is fun
- happy rendering
- thank you for joining workshop and thanks for your attention